

Noise Measurement for Obtaining Optimum Point of Detection System by Using Field Effect Transistor (FET)

أفضل نقطة حساب للضوضاء في أنظمة الكشف باستخدام ترانستور ذات المجال المؤثر (FET)

L.Haider Khder Lateef A.L. Mukhalad Kadom Marza A.L. Mohanned Hassan Ali
Department Engineering of
Technical Electrical Power
Technical College/ Musayab

Abstract:

The designed circuit in this research is measured several types of noise and it's analysis, reduction and amplification of received signal value by using the detection system type Field Effect Transistor (FET Tr) the aim of using this type of amplifier in designed system because of it's efficient matching between input and output impedance, this will increase performance in detection of signal and noise. Also, all equations that help in calculation of noise voltage and noise current are derived and effect of bias resistance and capacitance of detector also was studied. Research study shows that the preamplifier noise is primarily influence by the first stage noise provided that the gain of that stage is large ($K_t=8.87$), total noise voltage to detection system ($E_n T=3.314$ nV), total noise current ($I_n T=5.41$ fA), noise figure ($NF=0.0093$ dB) at optimum source resistance and the detector resistance (2.5 M Ω) photoconductive type.

الخلاصة:

يتناول هذا البحث تصميم دائرة قياس عدة أنواع للضوضاء وتحليلها، كيفية تقليلها وتكبير قيمة الإشارة المستلمة من قبل منظومة الكشف وتكبيرها بمكبرات نوع ترانستور ذات المجال المؤثر (FET Tr) والسبب في استخدام هذا النوع من المكبرات في المنظومة المصممة لكفائته في الموائمة بين ممانعة الإدخال والخراج مما يؤدي الى زيادة الاداء في كشف الإشارة والضوضاء. كذلك تم اشتقاق المعادلات الخاصة لحساب قيم فولتية الضوضاء (E_n) وتيار الضوضاء (I_n) ودراسة تأثير مقاومة الانحياز والسعة على ضوضاء الإدخال للمنظومة، تحتوي الدائرة المصممة على كاشف نوع (photoconductive). وأظهرت نتائج الدراسة أن الضوضاء المكبر الأولي (preamplifier) تتأثر بشكل كبير بوضوء أول مرحلة تكبير وكانت ذات عامل ربح عالي ($K_t=8.87$) وفولتية الضوضاء الكلية لمنظومة الاستلام هي ($E_n T=3.314$ nV) وتيار الضوضاء الكلية ($I_n T=5.41$ fA) وكان رقم الضوضاء (noise figure) هو ($NF=0.0093$ dB) عند قيمة أفضل مقاومة مصدر، وقيمة مقاومة الكاشف (photoconductive detector resistance) بحدود (2.5 M Ω).

I. Introduction

The noise is originating from source fluctuation or of background radiation, photon noise associated with random arrival of photons from steady source; from the detector it self, or from the amplifying system. Back ground radiation makes important contribution to noise in IR because spectrometer and surrounding radiate at (10mm) (background ignored <1 μ m). Detectors noise comes from the dark current a single in the absence of incident radiation which thermal in origin [1].

However, we are interested only in the random electrical fluctuations generated in circuit elements and note in externally generated effects such as static, power supply and ignition noise [2].

The primary requirement is for anise figure that is so low that the noise from the detector is the limiting source of noise in the system. Unfortunately no signal preamplifier can provide optimum performance with all of the available detectors [3].

In the transistor noise model used by Vander Ziel shot [4] and (1/f) noise voltage generators are in series with the emitter; a thermal noise- voltage generator is in series with the base, shot and (1/f) noise

current generator are in parallel with the collector. A simplified noise model for use at frequencies above the (1/f) region had been carried out. [5].

II. Theory

The detector total noise (Vn) is given by:-

$$V_n = \sqrt{\sum_1^n V_{ni}^2} \dots\dots\dots (1)$$

Where (Vni) represents the particular noise source voltage (current) involved in the radiation detection process.

The typical frequency dependence of the detector noise current (voltage) is shown in fig (1). [6]. There are several types of noise:-

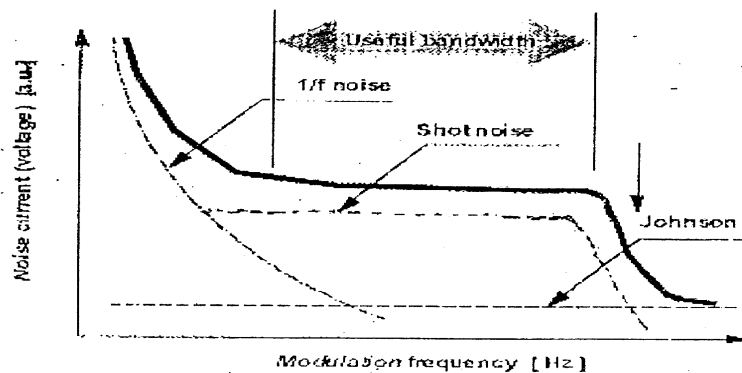


Fig. (1) Noise Sources

II.I. Low Frequency or (1/f) Noise

At low frequency there are several types of noise for which the power spectrum varies inversely with frequency. Since this (1/f) noise is greater than, or in excess of shot noise, it's sometimes called excess noise. It is called modulation noise in semiconductors, such as transistors and photo detector, contact noise in carbon resistors and their electrical contacts; and flicker noise in vacuum- tube cathode. In most devices the (1/f) noise becomes negligible with respect to other types of noise at frequencies above a few hundred H Z [7, 8].

II.II. Excess Noise

Many resistors also exhibit excess noise when direct current is present. This noise contribution is greatest in composition carbon resistors and is usually not important in wire wound resistors. Excess noise is so named because it is present in addition to the fundamental thermal noise of the resistor [8].

II.III. Thermal Noise [3, 9]

In 1928 Johnson showed experimentally that a resistor acts as a generator of noise having a mean-square – voltage.

$$E_t^2 = 4K.T.R.\Delta f \dots\dots\dots (2)$$

where

K= Boltzman constant = 1.38×10^{-23} w.sec/k

T= temperature of the conduction in (k)

R= its resistance in (Ω).

Δf = noise band with of the measuring system in HZ.

A more complete expression for thermal noise is:-

$$E_t^2 = 4K.T.R.P(f).\Delta f$$

where

$p(f)$ is referred to as the plank factor: [7]

$$P(f) = (h.f/K.T). (e^{h.f/K.T} - 1)^{-1}$$

and $h = 6.62 \times 10^{-34}$ J.sec , in plank's constant.

When designing a system, frequency limiting can be incorporated in of the later stages. For a laboratory application, frequency limiting can be obtained from wave analyzers, tuned voltmeters and filters. It is usually undesirable to do the frequency limiting with the sensor or the i/p – coupling network. This tends to decrease signal and sensor noise, but it does not attenuate the amplified noise that is generated following the coupling network [9].

II.IV. Thermal Noise Equivalent Circuit

In order to perform a noise analysis of an electronic system every element that generates thermal noise is represented by an equivalent cct composed of a noise voltage generator in series with a noiseless resistance (R) connected between terminals (a) and (b). As shown in fig (2)[7].

$$I_t = (4KTD_f/R)^{1/2} \dots\dots\dots (3)$$

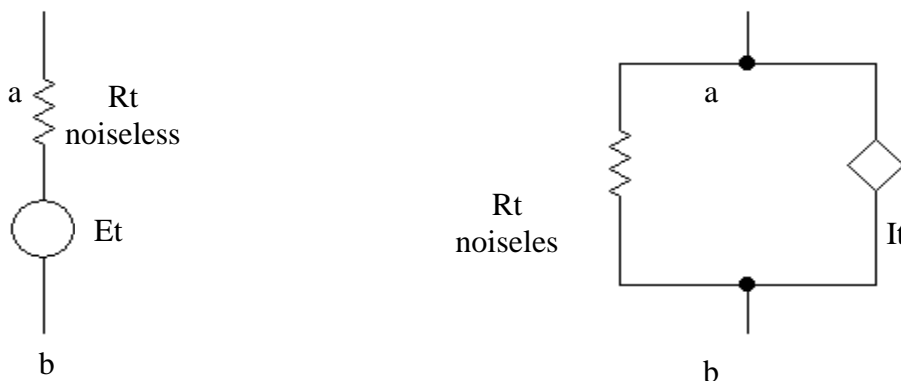


Fig. (2) Equivalent circuits for Thermal Noise

II.V. Shot Noise

In tubes, transistors and diodes there is a noise mechanism called shot noise. Considering the case of vacuum tube diode with high plate voltage so that all the electrons emitted from cathode are collected. The r.m.s value of the shot noise current is observed to be given by [7].

$$I_{sh} = \sqrt{2q.I_{dc}.\Delta f} \dots\dots\dots (4)$$

where

q = electronic charge ($1.6 \times 10^{-19} c$)

I_{dc} =direct current in A.

Δf =noise band width in HZ.

III. Amplifier Noise

Since every electrical component is potential source of noise, a network such as an amplifier that contains many components could be difficult to analyze from a noise stand point.

III.I. Noise Voltage and Current Model

There are universal noise models for any two-part network. This noise model, shown in fig(3),is used to represent an amplifier; it can also apply to passive ccts, tubes, transistors, tunnel diodes,

integrated circuit (Ic) amplifiers, and so on. Figure also includes the signal source Vs and noisy source

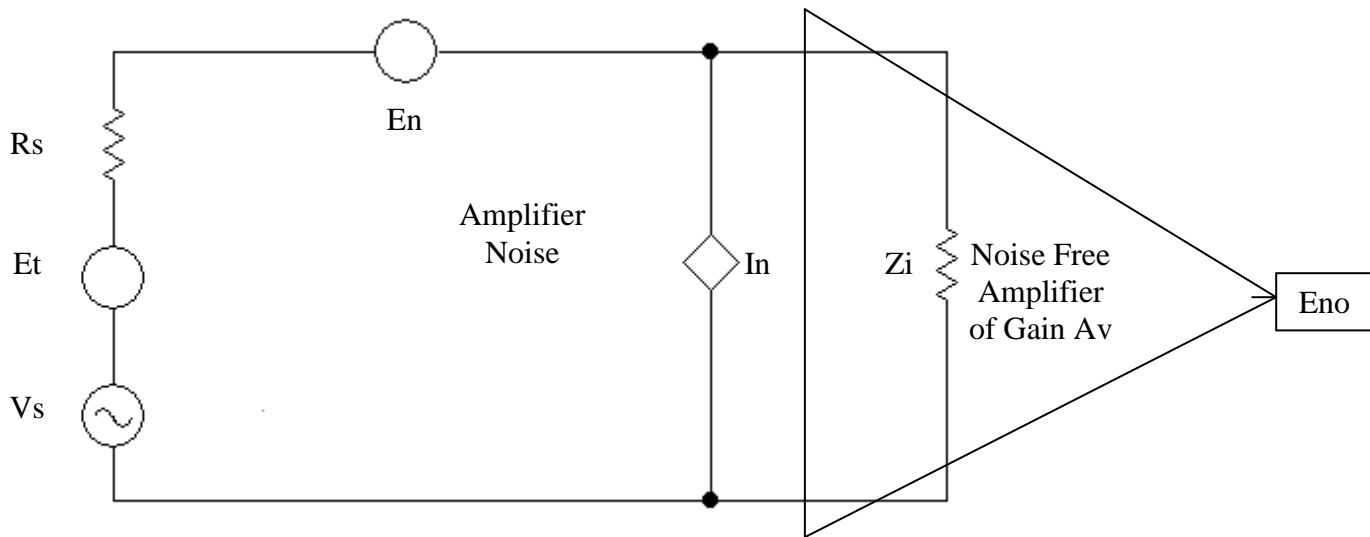


Fig. (3) Amplifier Noise Model and Signal Noise Source

III.II. Equivalent Input Noise [7]

Although the number of the noise sources have been reduced to three sources in the system shown in fig(3) by using the(En-In) model for the electronic circuitry, additionally simplification can be used (equivalent input noise) Eni. This parameter refers all noise sources to the signal source location. The total noise in the output part is,

$$Eno^2 = Av^2 \cdot Eni^2 \dots\dots\dots (5)$$

Therefore

$$Eno^2 = Av^2 \cdot [(En^2 + Et^2) \cdot Zi^2 / (Rs + Zi)^2 + In^2 \cdot Zi^2 \cdot Rs^2 / (Rs + Zi)^2] \dots\dots\dots (6)$$

The transfer function from i/p source to o/p is called system gain Kt. by definition,

$$Kt = Vo / Vi \dots\dots\dots (7)$$

Note that (Kt) is different from the voltage gain (Av); it is dependent on both amplifier i/p impedance and generator impedance and varies with frequency.

The r.m.s o/p signal can be expressed by:

$$Vo = Av \cdot Vs \cdot Zi / (Rs + Zi) \dots\dots\dots (8)$$

Sub. Equ(8) into equ(7) gives an expression for the system gain Kt in terms of network parameters;

$$Kt = Av \cdot Zi / (Rs + Zi) \dots\dots\dots (9)$$

The total o/p noise given in equ(6) divided by the system gain given in equ(9) yield an expression for equivalent i/p noise;

$$Eno^2 / Kt^2 = Eni^2 \dots\dots\dots (10)$$

The expression for equivalent i/p noise is;

$$Eni^2 = Et^2 + En^2 + In^2 \cdot Rs^2 \dots\dots\dots (11)$$

This equation is important for the analysis of many noise problems.

Amplifier i/p resistance and capacitance are not present in the equivalent i/p noise expression. A noise analysis is some what simplified when the loading caused by the amplifier i/p impedance is neglected.

III.III. Noise Figure:

Noise factor, F, also called figure; is a figure-of-merit for a device or a cct with respect to noise.

[11] This definition of noise factor in equ. form is;

$$F = (i/p \text{ signal-to-noise}) / (o/p \text{ signal-to-noise}) = (S_i/N_i) / (S_o/N_o) \dots\dots\dots(12)$$

The logarithmic expression for noise figure Nf is

$$Nf = 10 \text{Log } F \dots\dots\dots (13)$$

The noise figure Nf can be defined in terms of En and In.

Thus

$$Nf = 10 \text{Log } (En^2/Et^2) = 10 \text{log } (Et^2 + En^2 + In^2 \cdot R_s^2 / Et^2) \dots\dots\dots (14)$$

III.IV. Optimum Source Resistance

The point at which total equivalent i/p noise approaches closest to the thermal noise. At this point, the amplifier adds minimum noise to the thermal noise of the source; the noise figure reaches a minimum value.

This optimum source resistance is called (Ro/p) or (Ro) and may be obtained from [12].

$$R_o = E_n / I_n \quad / \quad E_n = I_n \cdot R_s \dots\dots\dots (15)$$

The value of noise factor at this point can be called Fo/p.

Rearrangement of equ.(14) can yield,

$$F_{o/p} = 1 + E_n \cdot I_n / 2K \cdot T \cdot \Delta_f \dots\dots\dots (16)$$

Optimum source resistance, Ro, is not the resistance for maximum power transfer. There is no direct relation between Ro and the amplifier i/p impedance Zi. Ro determined by the amplifier noise mechanisms and has bearing on the maximum signal to noise ratio.

III.V. Noise in Cascaded Network

It can be considered now the problem of locating the important noise source within a system. By deriving a usable expression for the noise factor of cascaded network in terms of the characteristic of each network.

The system to be analyzed is shown in fig (4) [12].

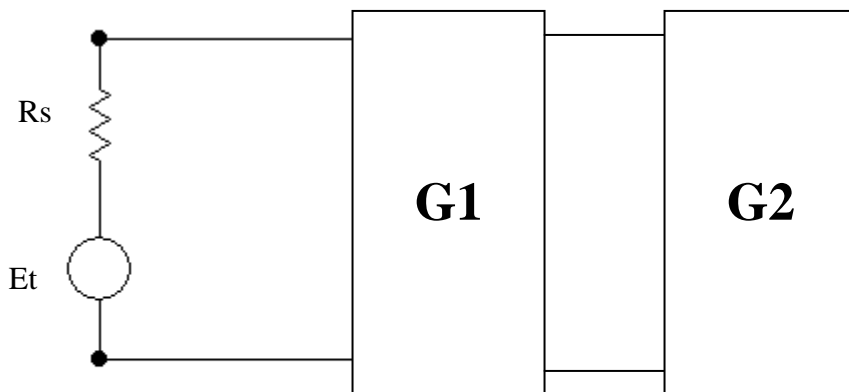


Fig. (4) Cascaded Network

It consist of a signal source with internal thermal noise and two cascaded net works equ.(12) gives noise factor as the S/N.

The available thermal noise power is (Ni=Et²/4Rs), therefore an alternate expression for (F) is;

$$F = N_o / G_a \cdot K \cdot T \cdot \Delta_f \dots\dots\dots (17)$$

Where no available noise power at the load terminals. equ.(2-17) is not useful design equation in it's present form because both (N_o and G_a) are unknown parameters. the available noise power at the i/p to network (N_{i2}) is;

$$N_{i2} = N_{o1} = F_1 \cdot G_1 \cdot K \cdot T \cdot \Delta_f \quad \dots\dots\dots (18)$$

$$F_2 = N_{o2} / G_2 \cdot K \cdot T \cdot \Delta_f \quad \dots\dots\dots (19)$$

The noise originating in the second stage is ($N_{o2} - G_2 \cdot K \cdot T \cdot \Delta_f$) or from equ (2-19) it is;

$$F_2 \cdot G_2 \cdot K \cdot T \cdot \Delta_f - G_2 \cdot K \cdot T \cdot \Delta_f = (F_2 - 1) \cdot G_2 \cdot K \cdot T \cdot \Delta_f \quad \dots\dots\dots (20)$$

The total o/p noise (N_{oT}) is given by the sum of terms from equ (18) and equ (20);

$$N_{oT} = G_2 \cdot (F_1 \cdot G_1 \cdot K \cdot T \cdot \Delta_f) + (F_2 - 1) \cdot G_2 \cdot K \cdot T \cdot \Delta_f \quad \dots\dots\dots (21)$$

The noise factor of the cascaded pair is;

$$F_{12} = N_{oT} / G_1 \cdot G_2 \cdot K \cdot T \cdot \Delta_f \quad \dots\dots\dots (22)$$

By sub. Of equ (21) in to equ (22):

$$F_{12} = F_1 + F_2 - 1 / G_1$$

If the analysis is extended to three-stage; we obtained the classic relation developed by Friis [13].

$$F_{123} = F_1 + F_2 - 1 / G_1 + F_3 - 1 / G_1 \cdot G_2 \quad \dots\dots\dots (23)$$

One concludes then that the noise factor of a cascaded network is primarily influenced by first-stage noise; provide that the gain of that stage is large.

IV. Procedure and Tools

The equipment used in this test is as following:

1. Precision current source (0-20) A, optronic Laboratories Inc. This current source was used to operate the tungsten ribbon lamp, at (15A) D.C.
2. Spectral radiance standard, model 550, optronic laboratories Inc.as shown in fig (5).
3. Infrard spectro-radiometer, model 746; the grating type used is G-40-150, the monochromater will scan wavelength.

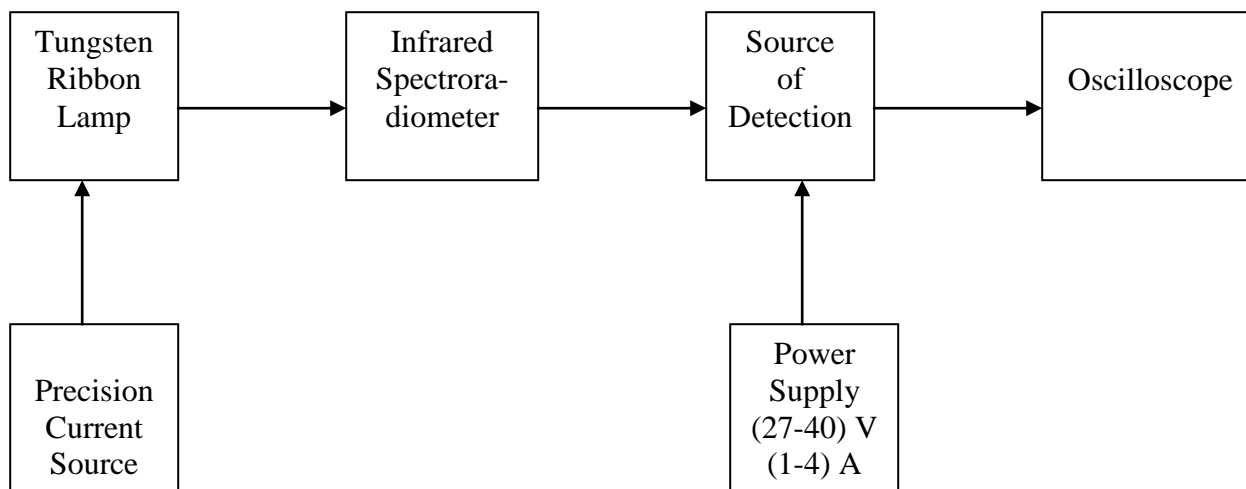


Fig. (5) Spectral Response Test Set [14]

4. The source of detection (type of Si detector mustsubishi).
 5. Oscilloscope type synchrosops,model SS-6421,dc-350MHZ,JAPAN.
- To measure the current-voltage characteristic (c/cs), the circuit that connected as shown in fig (6).

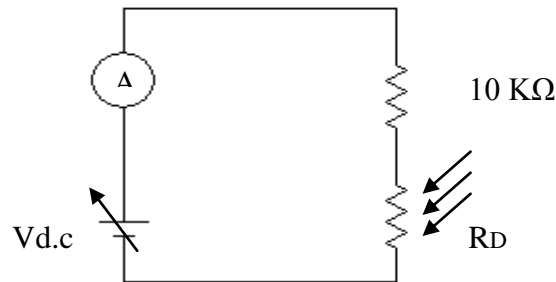


Fig. (6) Test Set For V-I (c/cs)

The d.c power supply $V_{d.c}$ used in this test is HP6337B, (0-25) V, (0-2) A, and the ammeter (A) type, is Fluke; model 8010 A digital multimeter. To measure the transfer voltage gain (K_t) at various frequencies a function generator (V_s) was inserted in series with source impedance (sensor), and the signal (V_o) was measured. Transfer voltage gain (K_t) is the ratio of V_o to V_s .

The test is set as shown in fig (7). A voltage divider composed of two resistors (each 56Ω) was connected across i/p terminals of the function generator to avoid the amplifier saturation, operational amplifier type (TL084).

The function generator type is (HP) model 8816 A (50 MHZ).

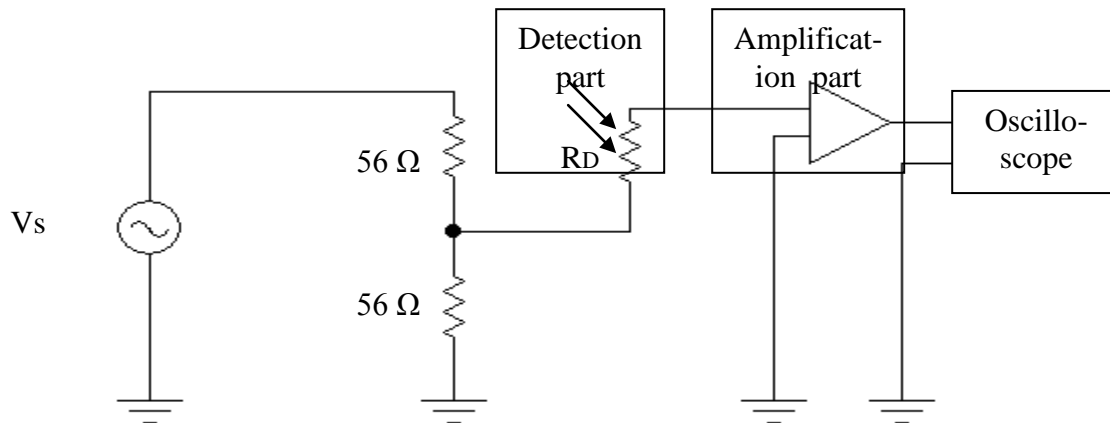


Fig. (7) Amplifier Frequency Response Measurement

V. Results and Discussions

The low noise design concerned with the following problem:

Given a sensor with known signal, noise, impedance and response characteristics (c/cs). Now how to optimize the amplifier design to achieve the lowest value of equivalent i/p noise?

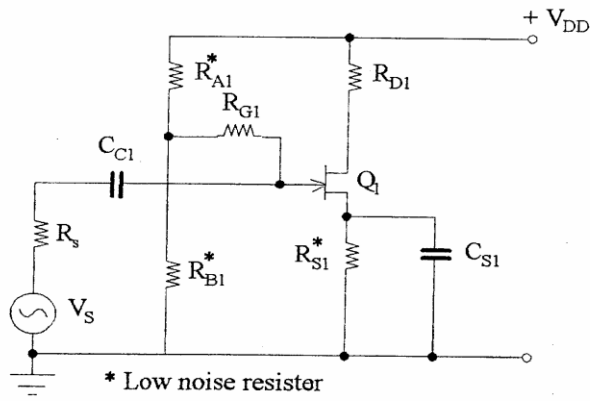
1. Amplification portion of the system must be matched to the sensor. This matching is the essence of low-noise design.
2. Sensor impedance and the first stage (Q), of the amplifier determine the ultimate limit on equivalent input noise.
3. Source impedance $Z_{s(f)}$ and noise generator $E_{n(f)}$ and $I_{n(f)}$ representing Q1 are each a different function of frequency.
4. Initial steps in the design procedure are the selection of the type of input device, such as bipolar transistor, FET or Ic, and the associated operating point to obtain the desire noise c/cs. After selecting i/p stage the circuit (cct) is design.
5. Noise in FFT device was introduced in the theory. Because of the high impedance of the sensor used in our application, the FFT is an attractive i/p device[8]. In the common source (cs) configuration infinite i/p impedance. The circuit (cct) diagram of this connection is shown in fig (8-a); the gate to channel diode of this n-channel FET is reversed biased.
6. The biasing network contains a resistance (RG1) connected between the junction of (RA1), and (RB1), and the FET gate. Fig (8-b) shows the small signal (ac) and noise equivalent cct for this connection. The voltage gain provide by the (cs) is.

$$K_t = g_m \cdot R_L / (1 + g_m \cdot Z_{s1}) \dots\dots\dots (24)$$

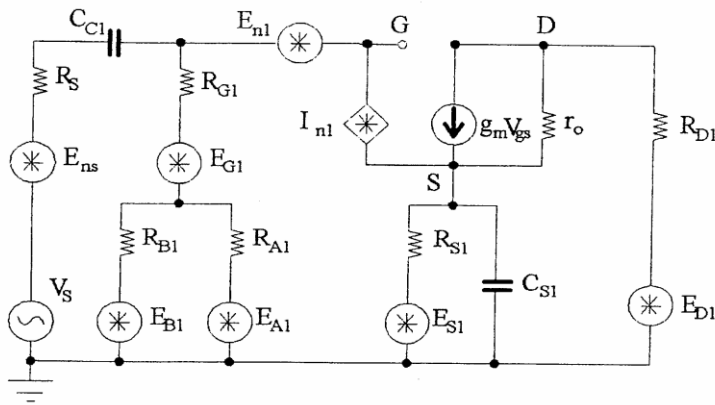
Where $R_L = R_{D1} // r_o$

$$Z_{s1} = R_{s1} // -j \cdot X_{s1}$$

The equivalent input noise is equal [11];



(a)



(b)

Fig. (8): Parallel CS Amplifier: (b): Noise Equivalent

$$E_{ni}^2 = E_{ns}^2 + E_n^2 (R_G + R_S / R_G)^2 + I_n^2 (R_{sj} \cdot X_{c1})^2 + [E_{A1}^2 (R_{B1} / R_{A1})^2 + E_{B1}^2 (R_{A1} / R_{B1})^2 + E_{G1}^2] \cdot R_S^2 / R_{G1}^2 + (E_{s1} / w \cdot R_{s1} \cdot C_{s1})^2 + E_{D1}^2 / K_{t1}^2 \dots \dots \dots (25)$$

The source by pass capacitor C_{s1} determines the break frequency f . the angular frequency at which the voltage gain is (3dB) below the mid frequency value is;

$$W_L = 1 / C_{S1} \cdot R_{S1} \cdot [r_o + R_{D1} / (g_m \cdot r_o + 1) \cdot R_{S1} + r_o + R_{D1}] \dots \dots \dots (26)$$

7.The frequency response for detection system preamplifier as shown in fig (9).the amplifier has a peak gain response at (72) dB; the gain response has a sharp low cut-off frequency at about (1040) HZ.this will attenuate the (1/f) noise originates in the sensor and the i/p stage of the preamplifier.

The result of detector (V-I) c/cs is shown in fig (10). The detector has linear c/cs over voltage range (2-24) V under dark condition. The curve indicates that the sensor is photo conductive detector having a resistance about (2.4 MΩ). The measured capacitance is about (0.165 μf) which represent the sum of series and shunt wiring capacitance.

The spectral response of detection system in the amplifier as shown in fig (11); the curve has a peak value at (3.9 μm). For common stage shown in fig (8).

The dc-load-line equation

$$V_{DD} = V_{DS} + i_D (R_{D1} + R_{S1}) \dots \dots \dots (27)$$

and the gate voltage is:-

$$V_{GS} = (R_{B1} / R_{A1} + R_{B1}) \cdot V_{DD} + i_D \cdot R_{S1} \dots \dots \dots (28)$$

To design the amplifier for a (Q-point) at ($V_{DS}=5$ V) and ($I_{DQ}=1$ mA); sub these values ($V_{DD}=15$ V) in to equ. (27):-

$$R_{D1} + R_{S1} = V_{DD} + V_{DSQ} / I_{DQ} = 10 \text{ K}\Omega$$

Optimum amplification value for resistance R_{S1} & R_{D1} is ($R_{S1}=4.9$ KΩ) and ($R_{D1}=4.9$ KΩ); then ($I_D=.97$ mA) the Q-point occurs at a gate-to-source voltage:-

$$V_{GSQ} = -0.25 \text{ V}$$

Then; using equ. (28) getting:-

$$(R_{B1} / R_{A1} + R_{B1}) \cdot V_{DD} = 5 \text{ V}$$

For ($R_{A1}=1$ MΩ); then ($R_{B1}= 490$ KΩ)

For cct diagram shown in fig (8); the i/p noise E_{ni} was given in equ.(25); to get the preamplifier i/p noise calculation.

This equ.can be separated in to two parts, E_{nT} and I_{nT} .

$$\text{For } R_S \rightarrow 0 \quad E_{nT}^2 = E_{ni}^2 + I_{ni}^2 \cdot X_{c1}^2 + (E_{s1} / w \cdot R_{s1} \cdot C_{s1})^2 + E_{D1}^2 / K_{t1}^2 \dots \dots \dots (29)$$

And for $R_S \rightarrow (\infty)$

$$I_{nT}^2 = I_{ni}^2 + [E_{A1}^2 \cdot (R_{B1} / R_{A1})^2 + E_{B1}^2 \cdot (R_{A1} / R_{B1})^2 + E_{G1}^2] \cdot 1 / R_{G1}^2 \dots \dots \dots (30)$$

For $R_{G1}=10^9 \Omega$; $C_{s1}=22 \mu f$; $C_{c1}=33 \text{ nf}$; $r_o=20 \text{ K}\Omega$ typical value

From equ.(24), then $K_{t1}=8.7$

By using equ.(2):- $4K \cdot T=1.6 \cdot 10^{-20}$ (at room temperature 290 K)

The thermal noise levels in $R_{A1}, R_{B1}, R_{G1}, R_{D1}, R_{S1}$ are:-

$$E_{A1} = (1.6 \cdot 10^{-14})^{1/2} = 126 \text{ nV}$$

$$E_{B1} = (7.52 \cdot 10^{-15})^{1/2} = 87 \text{ nV}$$

$$E_{G1} = (1.6 \cdot 10^{-11})^{1/2} = 4 \mu V$$

$$E_{D1} = (8.16 \cdot 10^{-17})^{1/2} = 9 \text{ nV}$$

$$E_{S1} = (8.16 \cdot 10^{-17})^{1/2} = 9 \text{ nV}$$

the terms in equ.(27) are :-

$$E_{n1} = 3.16 \text{ nV} \rightarrow Z_{n1} \cdot X_{c1} = 0.014 \text{ nV}$$

$$I_{nT} = 5.31 \text{ fA}$$

The optimum source resistance is: - $R_o = E_{nT} / I_{nT} = 625 \text{ K}\Omega$

Using equ.(14), the noise figure at R_o is :-
 $NF=0.0093$ dB

The measurement frequency response for the preamplifier having the above component values is shown in fig (12). This measurement was done at i/p r.m.s voltage level of (7 mV).the o/p r.m.s voltage was (72 mV) at (1.2 KHZ).

The static drain current of Q1 ($I_{Ds}= 0.98$ mA) is at relatively high level. The reason for operating at high level of I_D was given in the theoretical part, to minimize the (E_n) parameter.Unfortunaly; this selection for I_D results in relatively low values for the drain load resistor (R_D).since voltage gain in the connection proportional to (R_D), we are not able to develop high gain in the i/p stage. After selection the i/p stage the cct is design. The biasing is set up, and the coupling network is determined; then the total noise of the entire system is analyzed; including the bias network contributions to ensure the design still meet the noise specifications.

At high values of source resistance (FET) are more desirable because of their very low noise current (I_n). In some instances they are even preferred when low E_n is desired. A good (FET) has E_n slightly larger then that of a bipolar (Tr), and it's (I_n) is significantly lower. Another advantage of the (FET) is it's high i/p resistance and low capacitance; thus it's particularly useful as a voltage amplifier.

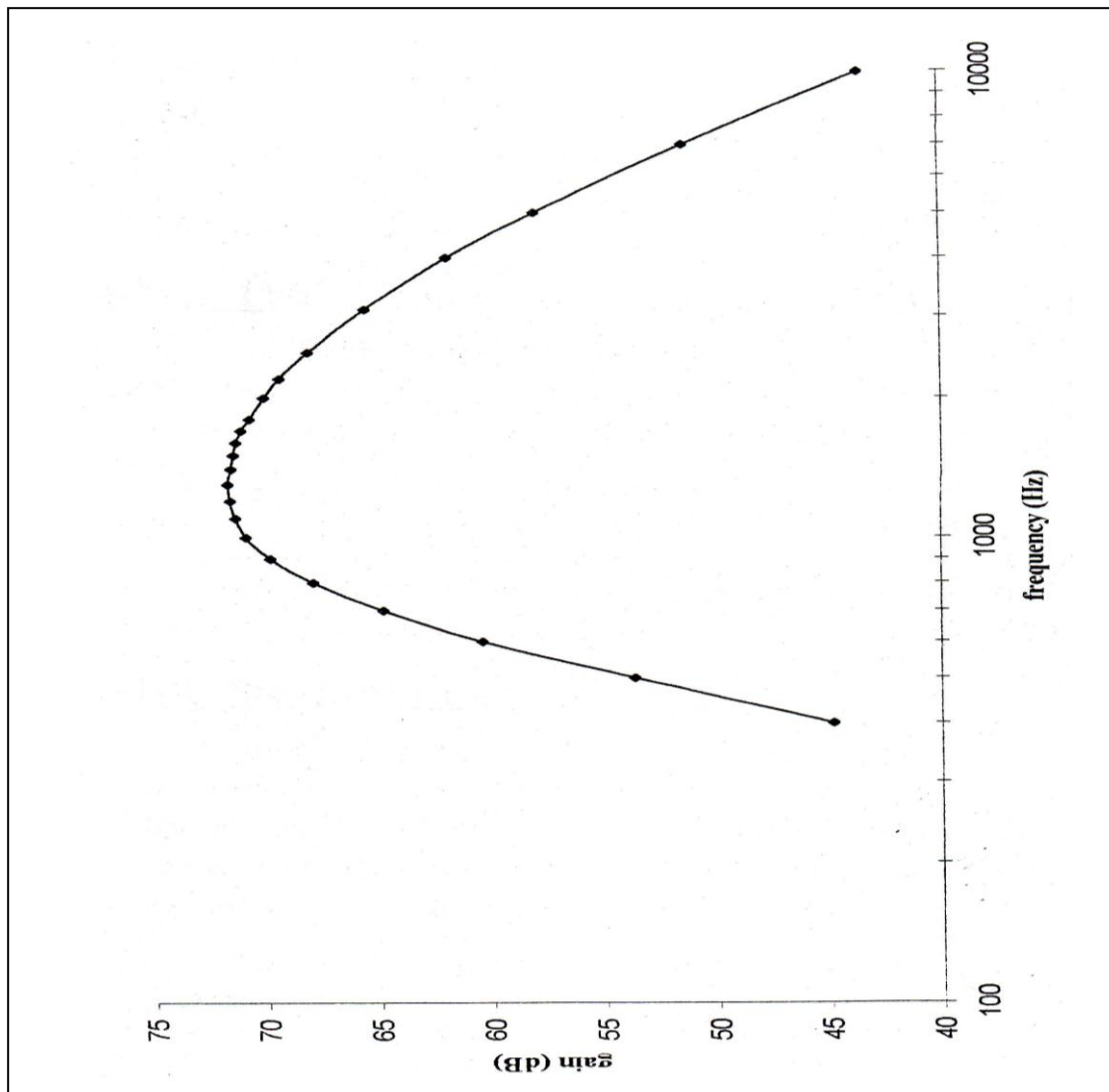


Fig.(9) Frequency Response for Detection System Preamplifier .

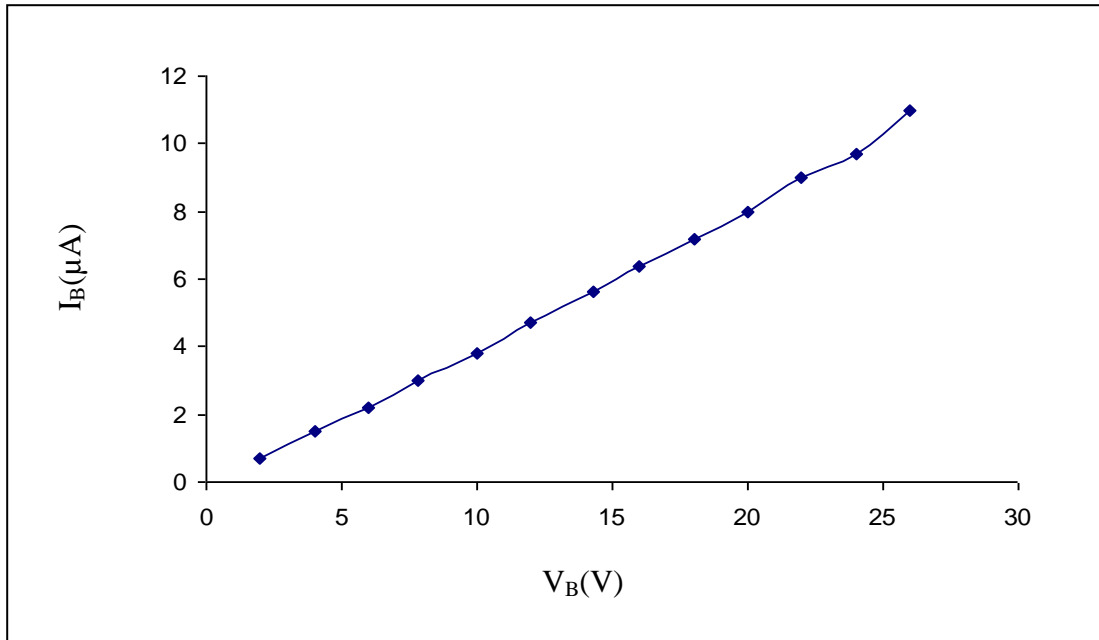


Fig.(10) Current – Voltage Characteristics .

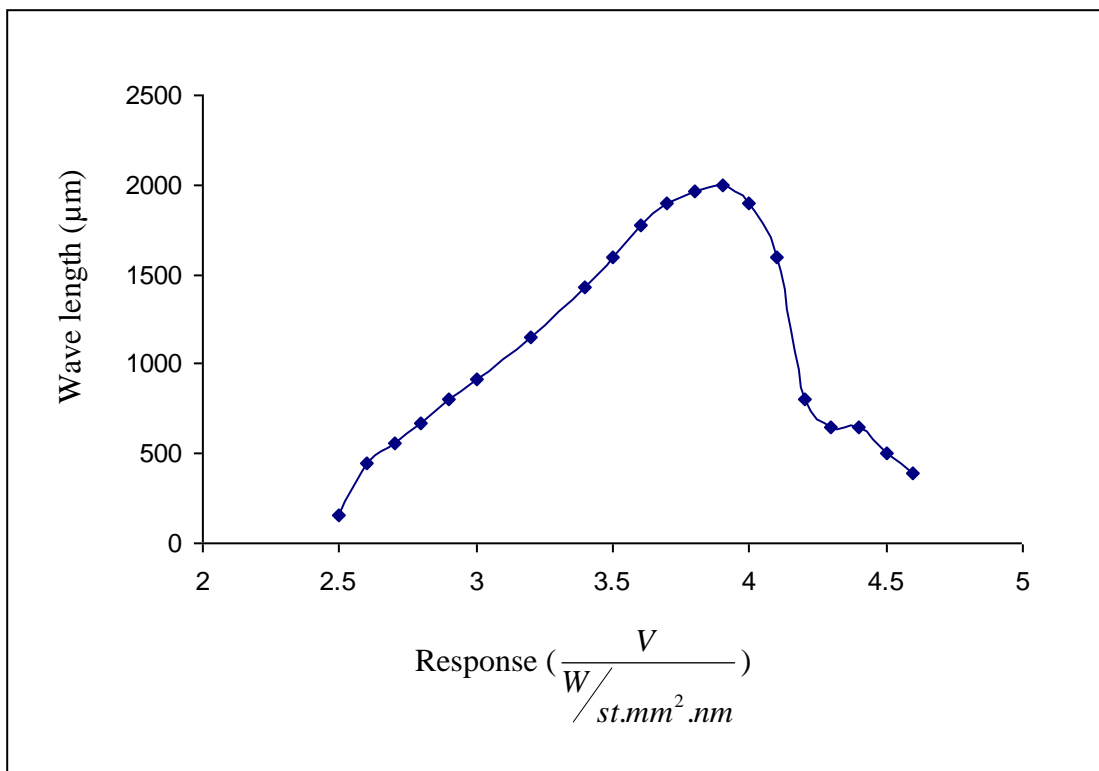


Fig.(11) Spectral Response for Detection System in the Amplifier .

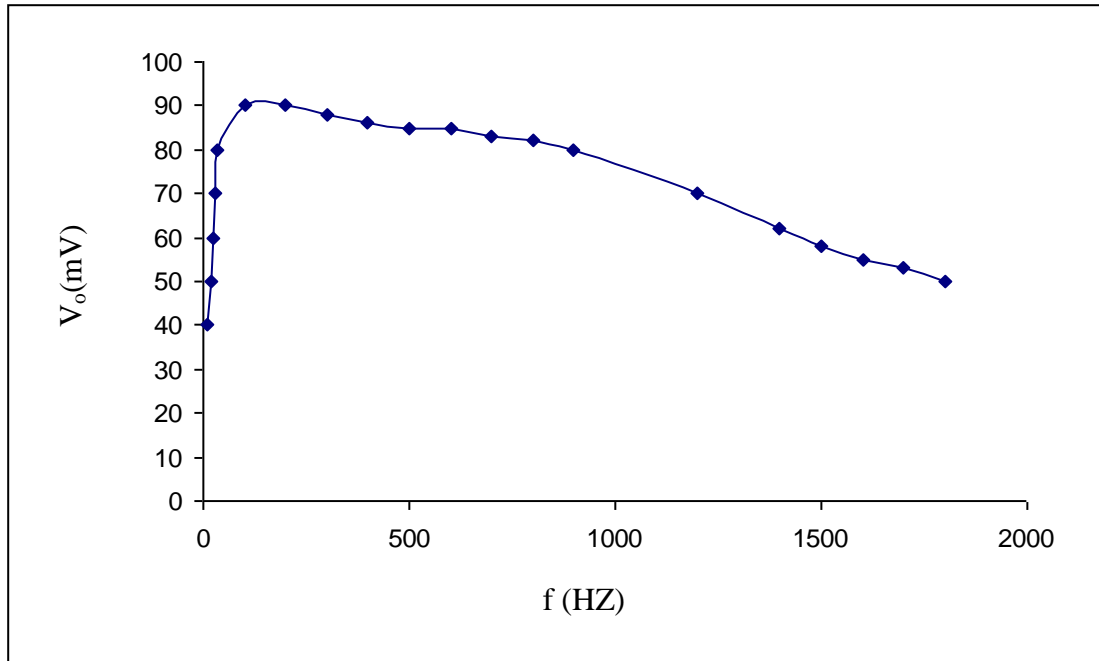


Fig.(12) Frequency response for the Designed Preamplifier .

References:

1. J.Pierce “physical source of noise”; V66, P612. (1956).
2. J.D.Vincent, “fundamentals of infrared detector operation and testing”,Santa Barbara research centrer, CH8; P213,(1989).
3. Richard D.Huda “infrared system engineering”,John wiley and Sons (1969) ,ch3, P132.
4. A.Vander Ziel “noise aspects of low-frequency solid state circuit”, solid state design, 3, 20, (March 1986).
5. A.E Sanderson and R.G. fulks,” A simplified noise theory and it’s application to the design of low-noise-amplifier”; IEEE Transf.Audio, Avg,106,(2003).
6. B. Livada “infrared detectors, characteristic and testing”; course lecture notes, P4-3,4-21(2006).
7. A. vander ziel;”noise” prentice –Hell, Englewood cliffs, CH5; P203, (2007).
8. W.R.Bennett; “electrical noise”, newyork, McGrawo-Hill,(1977).
9. C.D. Motcheubacher and F.L.fitcher; “low noise electronic design”, John-Wiley and Sons (1972).
10. “Representation of noise in linear two ports”, Proc, IRE, 48, 1(Janury 1983).
11. “IRE standards on methods of measuring noise in linear two port,1986”, Proc. IRE,48,1,(January 1988) p(60-67).
- 12 A .Vander Zeil;”noise in measurements”,John-Wiely and Sons,CH5,P345,(1976).
13. Friis,H.F;”noise figures of radio receivers”,Proc.IRE,32,7,(July 1994), P(419-432).
14. R.L. Peteritz. “fundamentals of infrared detectors” Proc.inst. Radio Enqrs, P47.VIII(1989).